# Package 'twosigma'

October 14, 2022

Type Package

Title DE Analysis for Single-Cell RNA-Sequencing Data

Version 1.0.2

Date 2021-12-10

Maintainer Eric Van Buren <edvanburen@gmail.com>

**Description** Implements the TWO-Component Single Cell Model-Based Association Method (TWO-SIGMA) for gene-level differential expression (DE) analysis and DE-based gene set testing of single-cell RNA-sequencing datasets. See Van Buren et al. (2020) <doi:10.1002/gepi.22361> and Van Buren et al. (2021) <doi:10.1101/2021.01.24.427979>.

License AGPL-3

**Imports** multcomp (>= 1.4-13), glmmTMB, methods, pscl (>= 1.5.5), pbapply (>= 1.4.0), parallel (>= 3.6.3), doParallel (>= 1.0.15)

**Encoding** UTF-8

LazyData false

URL https://github.com/edvanburen/twosigma

BugReports https://github.com/edvanburen/twosigma/issues

RoxygenNote 7.1.0

Suggests testthat

NeedsCompilation no

Author Eric Van Buren [aut, cre], Yun Li [aut], Di Wu [aut], Ming Hu [aut]

**Repository** CRAN

Date/Publication 2021-12-13 09:40:02 UTC

## **R** topics documented:

adhoc.twosigma	2
lr.twosigma	3
lr.twosigma_custom	6
simulate_zero_inflated_nb_random_effect_data	9
test.vc.twosigma	11
twosigma	14
twosigmag	16
twosigma_custom	20
	23

## Index

adhoc.twosigma	adhoc.twosigma:	Perform	the	ad	hoc	method	described	in	TWO-
	SIGMA paper								

## Description

adhoc.twosigma: Perform the ad hoc method described in TWO-SIGMA paper

## Usage

```
adhoc.twosigma(
  count,
  mean_covar,
  zi_covar,
  id,
  weights = rep(1, length(count))
)
```

## Arguments

count	Vector of non-negative integer read counts.
mean_covar	Covariates for the (conditional) mean model. Must be a matrix (without an intercept column) or $= 1$ to indicate an intercept only model.
zi_covar	Covariates for the zero-inflation model. Must be a matrix (without an intercept column), $= 1$ to indicate an intercept only model, or $= 0$ to indicate no zero-inflation model desired.
id	Vector of individual-level ID's. Used as predictor in ANOVA model.
weights	weights, as in glm. Defaults to 1 for all observations and no scaling or centering of weights is performed. Passed into zeroinfl function.

## Value

P-value from the ANOVA F test.

#### lr.twosigma

## Examples

# Set Parameters to Simulate Some Data

```
nind<-10;ncellsper<-rep(50,nind)</pre>
sigma.a<-.5;sigma.b<-.5;phi<-.1</pre>
alpha<-c(1,0,-.5,-2);beta<-c(2,0,-.1,.6)
beta2<-c(2,1,-.1,.6)
id.levels<-1:nind;nind<-length(id.levels)</pre>
id<-rep(id.levels,times=ncellsper)</pre>
sim.seed<-1234
# Simulate individual level covariates
t2d_sim<-rep(rbinom(nind,1,p=.4),times=ncellsper)</pre>
cdr_sim<-rbeta(sum(ncellsper),3,6)</pre>
age_sim<-rep(sample(c(20:60),size=nind,replace = TRUE),times=ncellsper)</pre>
# Construct design matrices
Z<-cbind(scale(t2d_sim),scale(age_sim),scale(cdr_sim))</pre>
colnames(Z)<-c("t2d_sim","age_sim","cdr_sim")</pre>
X<-cbind(scale(t2d_sim), scale(age_sim), scale(cdr_sim))</pre>
colnames(X)<-c("t2d_sim","age_sim","cdr_sim")</pre>
# Simulate Data
sim_dat<-matrix(nrow=2,ncol=sum(ncellsper))</pre>
for(i in 1:nrow(sim_dat)){
   sim_dat[i,]<-simulate_zero_inflated_nb_random_effect_data(ncellsper,X,Z,alpha,beta2</pre>
   ,phi,sigma.a,sigma.b,id.levels=NULL)$Y
}
rownames(sim_dat)<-paste("Gene",1:2)</pre>
# Run adhoc.twosigma
adhoc.twosigma(sim_dat[1,],mean_covar = X,zi_covar=Z,id = id)
```

lr.twosigmaConvenient wrapper function for performing joint likelihood ratio tests<br/>using the TWO-SIGMA model.

## Description

Convenient wrapper function for performing joint likelihood ratio tests using the TWO-SIGMA model.

#### Usage

lr.twosigma(

```
count_matrix,
 mean_covar,
 zi_covar,
 covar_to_test,
 mean_re = FALSE,
 zi_re = FALSE,
 id,
 return_full_fits = TRUE,
 adhoc = FALSE,
 adhoc_thresh = 0.1,
 silent = FALSE,
 disp_covar = NULL,
 weights = rep(1, ncol(count_matrix)),
 control = glmmTMBControl(),
 ncores = 1,
 cluster_type = "Fork",
 chunk_size = 10,
 lb = FALSE
)
```

## Arguments

Matrix of non-negative integer read counts, with rows corresponding to genes and columns corresponding to cells. It is recommended to make the rownames the gene names for better output.
Covariates for the (conditional) mean model. Must be a matrix (without an intercept column) or a vector if a single covariate is being tested.
Covariates for the zero-inflation model. Must be a matrix (without an intercept column) or a vector if a single covariate is being tested.
Either a string indicating the column name of the covariate to test or an integer referring to its column position in BOTH the mean_covar and zi_covar matrices (if the two matrices differ using a string name is preferred). Argument is ignored if mean_covar and zi_covar are both a single covariate (that covariate is assumed of interest).
Should random intercepts be included in the (conditional) mean model?
Should random intercepts be included in the zero-inflation model?
Vector of individual-level ID's. Used for random effect prediction and the adhoc method but required regardless.
S
If TRUE, fit objects of class glmmTMB are returned. If FALSE, only objects of class summary.glmmTMB are returned. The latter require a much larger amount of memory to store.
Should the adhoc method be used by default to judge if random effects are needed?
Value below which the adhoc p-value is deemed significant (and thus RE are deemed necessary). Only used if adhoc==TRUE.

#### lr.twosigma

silent	If TRUE, progress is not printed.
disp_covar	Covariates for a log-linear model for the dispersion. Either a matrix or = 1 to indicate an intercept only model.
weights	weights, as in glm. Defaults to 1 for all observations and no scaling or centering of weights is performed. See ?glmmTMBControl.
control	Control parameters for optimization in glmmTMB.
ncores	Number of cores used for parallelization. Defaults to 1, meaning no paralleliza- tion of any kind is done.
cluster_type	Whether to use a "cluster of type "Fork" or "Sock". On Unix systems, "Fork" will likely improve performance. On Windows, only "Sock" will actually result in parallelized computing.
chunk_size	Number of genes to be sent to each parallel environment. Parallelization is more efficient, particularly with a large count matrix, when the count matrix is 'chunked' into some common size (e.g. 10, 50, 200). Defaults to 10.
lb	Should load balancing be used for parallelization? Users will likely want to set to FALSE for improved performance.

#### Value

A list with the following elements:

- fit\_null: Model fits under the null hypothesis. If return\_summary\_fits=TRUE, returns a list of objects of class summary.glmmTMB. If return\_summary\_fits=FALSE, returns a list of model fit objects of class glmmTMB. In either case, the order matches the row order of count\_matrix, and the names of the list elements are taken as the rownames of count\_matrix.
- fit\_alt: Model fits under the alt hypothesis of the same format as fit\_null.
- LR\_stat: Vector of Likelihood Ratio statistics. A value of 'NA' implies a convergence issue or other model fit problem.
- LR\_p.val: Vector of Likelihood Ratio p-values. A value of 'NA' implies a convergence issue or other model fit problem.
- adhoc\_include\_RE: Logical vector indicator whether the adhoc method determined random effects needed. If adhoc=F, then a vector of NA's.

#### Details

This function assumes that the variable being tested is in both components of the model (and thus that the zero-inflation component exists and contains more than an Intercept). Users wishing to do fixed effect testing in other cases or specify custom model formulas they will need to construct the statistics themselves using either two separate calls to twosigma or the lr.twosigma\_custom function. If adhoc=TRUE, any input in mean\_re and zi\_re will be ignored. If either model fails to converge, or the LR statistic is negative, both the statistic and p-value are assigned as NA.

#### Examples

# Set Parameters to Simulate Some Data

```
nind<-10;ncellsper<-rep(50,nind)</pre>
sigma.a<-.5;sigma.b<-.5;phi<-.1</pre>
alpha<-c(1,0,-.5,-2);beta<-c(2,0,-.1,.6)
beta2<-c(2,1,-.1,.6)
id.levels<-1:nind;nind<-length(id.levels)</pre>
id<-rep(id.levels,times=ncellsper)</pre>
sim.seed<-1234
# Simulate individual level covariates
t2d_sim<-rep(rbinom(nind,1,p=.4),times=ncellsper)</pre>
cdr_sim<-rbeta(sum(ncellsper),3,6)</pre>
age_sim<-rep(sample(c(20:60),size=nind,replace = TRUE),times=ncellsper)</pre>
# Construct design matrices
Z<-cbind(scale(t2d_sim),scale(age_sim),scale(cdr_sim))</pre>
colnames(Z)<-c("t2d_sim","age_sim","cdr_sim")</pre>
X<-cbind(scale(t2d_sim),scale(age_sim),scale(cdr_sim))</pre>
colnames(X)<-c("t2d_sim","age_sim","cdr_sim")</pre>
# Simulate Data
sim_dat<-matrix(nrow=2,ncol=sum(ncellsper))</pre>
for(i in 1:nrow(sim_dat)){
   sim_dat[i,]<-simulate_zero_inflated_nb_random_effect_data(ncellsper,X,Z,alpha,beta2</pre>
   ,phi,sigma.a,sigma.b,id.levels=NULL)$Y
}
rownames(sim_dat)<-paste("Gene",1:2)</pre>
# Run lr.twosigma
lr.twosigma(count=sim_dat[1,,drop=FALSE],mean_covar = X,zi_covar = Z,id=id,covar_to_test = 1)
```

lr.twosigma\_custom Convenient wrapper function for performing joint likelihood ratio tests with the TWO-SIGMA model using custom user-specified formulas.

## Description

Convenient wrapper function for performing joint likelihood ratio tests with the TWO-SIGMA model using custom user-specified formulas.

## Usage

```
lr.twosigma_custom(
   count_matrix,
   mean_form_alt,
   zi_form_alt,
   mean_form_null,
```

## lr.twosigma\_custom

```
zi_form_null,
id,
lr.df,
return_full_fits = TRUE,
disp_covar = NULL,
weights = rep(1, ncol(count_matrix)),
control = glmmTMBControl(),
ncores = 1,
cluster_type = "Fork",
chunk_size = 10,
lb = FALSE,
internal_call = FALSE
)
```

## Arguments

count_matrix	Matrix of non-negative integer read counts, with rows corresponding to genes and columns corresponding to cells. It is recommended to make the rownames the gene names for better output.
mean_form_alt	Custom two-sided model formula for the (conditional) mean model under the null. Formula is passed directly into glmmTMB with random effects specified as in the lme4 package. Users should ensure that the dependent variable matches the argument to the parameter "count."
zi_form_alt	Custom one-sided model formula for the zero-inflation model under the alterna- tive. Formula is passed directly into glmmTMB with random effects specified as in lme4.
<pre>mean_form_null</pre>	Custom two-sided model formula for the (conditional) mean model under the null. Syntax is as in mean_form_alt.
zi_form_null	Custom one-sided model formula for the zero-inflation model under the null. Syntax is as in zi_form_alt.
id	Vector of individual-level (sample-level) ID's. Used for random effect predic- tion but required regardless of their presence in the model.
lr.df	Degrees of Freedom for the constructed likelihood ratio test. Must be a non-negative integer.
return_full_fit	ts
	If TRUE, full fit objects of class glmmTMB are returned. If FALSE, only fit objects of class summary.glmmTMB are returned. The latter requires far less memory to store.
disp_covar	Covariates for a log-linear model for the dispersion. Either a matrix or = 1 to indicate an intercept only model.
weights	weights, as in glm. Defaults to 1 for all observations and no scaling or centering of weights is performed.
control	Control parameters for optimization in glmmTMB. See ?glmmTMBControl.
ncores	Number of cores used for parallelization. Defaults to 1, meaning no paralleliza- tion of any kind is done.

cluster_type	Whether to use a "cluster of type "Fork" or "Sock". On Unix systems, "Fork" will likely improve performance. On Windows, only "Sock" will actually result in parallelized computing.
chunk_size	Number of genes to be sent to each parallel environment. Parallelization is more efficient, particularly with a large count matrix, when the count matrix is 'chunked' into some common size (e.g. 10, 50, 200). Defaults to 10.
lb	Should load balancing be used for parallelization? Users will likely want to set to FALSE for improved performance.
internal_call	Not needed by users called lr.twosigma_custom directly.

#### Value

A list with the following elements:

- fit\_null: Model fits under the null hypothesis. If return\_summary\_fits=TRUE, returns a list of objects of class summary.glmmTMB. If return\_summary\_fits=FALSE, returns a list of model fit objects of class glmmTMB. In either case, the order matches the row order of count\_matrix, and the names of the list elements are taken as the rownames of count\_matrix.
- fit\_alt: Model fits under the alt hypothesis of the same format as fit\_null.
- LR\_stat: Vector of Likelihood Ratio statistics. A value of 'NA' implies a convergence issue or other model fit problem.
- LR\_p.val: Vector of Likelihood Ratio p-values. A value of 'NA' implies a convergence issue or other model fit problem.

## Details

This function is a wrapper for conducting fixed effect likelihood ratio tests with twosigma. There is no checking to make sure that the alt and null model formulas represent a valid likelihood ratio test when fit together. Users must ensure that inputted formulas represent valid nested models. If either model fails to converge, or the LR statistic is negative, both the statistic and p-value are assigned as NA.

#### Examples

# Set Parameters to Simulate Some Data

```
nind<-10;ncellsper<-rep(50,nind)
sigma.a<-.5;sigma.b<-.5;phi<-.1
alpha<-c(1,0,-.5,-2);beta<-c(2,0,-.1,.6)
beta2<-c(2,1,-.1,.6)
id.levels<-1:nind;nind<-length(id.levels)
id<-rep(id.levels,times=ncellsper)
sim.seed<-1234</pre>
```

# Simulate individual level covariates

```
t2d_sim<-rep(rbinom(nind,1,p=.4),times=ncellsper)
cdr_sim<-rbeta(sum(ncellsper),3,6)
age_sim<-rep(sample(c(20:60),size=nind,replace = TRUE),times=ncellsper)</pre>
```

```
# Construct design matrices
```

```
Z<-cbind(scale(t2d_sim),scale(age_sim),scale(cdr_sim))
colnames(Z)<-c("t2d_sim","age_sim","cdr_sim")
X<-cbind(scale(t2d_sim),scale(age_sim),scale(cdr_sim))
colnames(X)<-c("t2d_sim","age_sim","cdr_sim")
# Simulate Data
sim_dat<-matrix(nrow=2,ncol=sum(ncellsper))
for(i in 1:nrow(sim_dat)){
    sim_dat[i,]<-simulate_zero_inflated_nb_random_effect_data(ncellsper,X,Z,alpha,beta2
    ,phi,sigma.a,sigma.b,id.levels=NULL)$Y
}
rownames(sim_dat)<-paste("Gene",1:2)
# Run lr.twosigma_custom
lr.twosigma_custom(count=sim_dat[1,,drop=FALSE]
,mean_form_alt = count~X,mean_form_null = count~X[,-1]
,zi_form_alt = ~0,zi_form_null = ~0,id=id,lr.df=1)
```

## Description

Simulated zero-inflated negative binomial data with random effects

#### Usage

```
simulate_zero_inflated_nb_random_effect_data(
    ncellsper,
    X,
    Z,
    alpha,
    beta,
    phi,
    sigma.a,
    sigma.b,
    id.levels = NULL,
    sim.seed = NULL
)
```

## Arguments

ncellsper	Vector giving the number of cells per individual. Length of the vector is taken as the number of individuals.
Х	Covariate matrix (without intercept) for the (conditional) mean model.
Z	Covariate matrix (without intercept) for the zero-inflation model.
alpha	Column vector of true parameters from the zero-inflation model. Number of rows must match number of columns in Z.
beta	Column vector of true parameters from the (conditional) mean model. Number of rows must match number of columns in X.
phi	Overdispersion parameter for the negative binomial distribution (see details for more about parameterization).
sigma.a	Standard deviation for the zero-inflation model random intercept.
sigma.b	Standard deviation for the (conditional) mean random intercept.
id.levels	Individual-level IDs. If NULL set as 1,2, up to the number of individuals.
sim.seed	Random seed to be used. If NULL one will be randomly chosen.

## Value

Y Simulated counts

X Covariate matrix (without intercept) for the (conditional) mean model.

Z Covariate matrix (without intercept) for the zero-inflation model.

a Random effects for the zero-inflation model.

b Random effects for the (conditional) mean model.

alpha Column vector of true parameters from the zero-inflation model. Number of rows must match number of columns in Z.

beta Column vector of true parameters from the (conditional) mean model. Number of rows must match number of columns in X.

phi Overdispersion parameter for the negative binomial distribution (see details for more about parameterization).

sigma.a Standard deviation for the zero-inflation model random intercept.

sigma.b Standard deviation for the (conditional) mean random intercept.

nind Number of individuals.

ncellsper Vector giving the number of cells per individual.

id.levels Individual-level IDs.

## Examples

# Set Parameters to Simulate Some Data

```
nind<-10;ncellsper<-rep(50,nind)
sigma.a<-.5;sigma.b<-.5;phi<-.1
alpha<-c(1,0,-.5,-2);beta<-c(2,0,-.1,.6)</pre>
```

## test.vc.twosigma

```
beta2<-c(2,1,-.1,.6)
id.levels<-1:nind;nind<-length(id.levels)</pre>
id<-rep(id.levels,times=ncellsper)</pre>
sim.seed<-1234
# Simulate individual level covariates
t2d_sim<-rep(rbinom(nind,1,p=.4),times=ncellsper)</pre>
cdr_sim<-rbeta(sum(ncellsper),3,6)</pre>
age_sim<-rep(sample(c(20:60),size=nind,replace = TRUE),times=ncellsper)</pre>
# Construct design matrices
Z<-cbind(scale(t2d_sim),scale(age_sim),scale(cdr_sim))</pre>
colnames(Z)<-c("t2d_sim","age_sim","cdr_sim")</pre>
X<-cbind(scale(t2d_sim),scale(age_sim),scale(cdr_sim))</pre>
colnames(X)<-c("t2d_sim","age_sim","cdr_sim")</pre>
# Simulate Data
sim_dat<-matrix(nrow=2,ncol=sum(ncellsper))</pre>
for(i in 1:nrow(sim_dat)){
   sim_dat[i,]<-simulate_zero_inflated_nb_random_effect_data(ncellsper,X,Z,alpha,beta2</pre>
   ,phi,sigma.a,sigma.b,id.levels=NULL)$Y
}
rownames(sim_dat)<-paste("Gene",1:2)</pre>
```

test.vc.twosigma	Convenient wrapper function for performing (joint) likelihood ratio
	tests of variance components using the TWO-SIGMA model.

## Description

Convenient wrapper function for performing (joint) likelihood ratio tests of variance components using the TWO-SIGMA model.

#### Usage

```
test.vc.twosigma(
  count_matrix,
  mean_covar,
  zi_covar,
  mean_re = TRUE,
  zi_re = TRUE,
  id,
  return_full_fits = TRUE,
  adhoc = FALSE,
  adhoc_thresh = 0.1,
  silent = FALSE,
```

```
disp_covar = NULL,
weights = rep(1, ncol(count_matrix)),
control = glmmTMBControl(),
ncores = 1,
cluster_type = "Fork",
chunk_size = 1,
lb = FALSE
)
```

## Arguments

count_matrix	Matrix of non-negative integer read counts, with rows corresponding to genes and columns corresponding to cells. It is recommended to make the rownames the gene names for better output.
mean_covar	Covariates for the (conditional) mean model. Must be a matrix (without an intercept column) or a vector if a single covariate is being tested.
zi_covar	Covariates for the zero-inflation model. Must be a matrix (without an intercept column) or a vector if a single covariate is being tested.
mean_re	Should random intercepts be tested in the (conditional) mean model?
zi_re	Should random intercepts be tested in the zero-inflation model?
id	Vector of individual-level ID's. Used for random effect prediction and the adhoc method but required regardless.
<pre>return_full_fit</pre>	S
	If TRUE, fit objects of class glmmTMB are returned. If FALSE, only objects of class summary.glmmTMB are returned. The latter require a much larger amount of memory to store.
adhoc	Should the adhoc method be used by default to judge if random effects are needed?
adhoc_thresh	Value below which the adhoc p-value is deemed significant (and thus RE are deemed necessary). Only used if adhoc==TRUE.
silent	If TRUE, progress is not printed.
disp_covar	Covariates for a log-linear model for the dispersion. Either a matrix or $= 1$ to indicate an intercept only model.
weights	weights, as in glm. Defaults to 1 for all observations and no scaling or centering of weights is performed. See ?glmmTMBControl.
control	Control parameters for optimization in glmmTMB.
ncores	Number of cores used for parallelization. Defaults to 1, meaning no parallelization of any kind is done.
cluster_type	Whether to use a "cluster of type "Fork" or "Sock". On Unix systems, "Fork" will likely improve performance. On Windows, only "Sock" will actually result in parallelized computing.
chunk_size	Number of genes to be sent to each parallel environment. Parallelization is more efficient, particularly with a large count matrix, when the count matrix is 'chunked' into some common size (e.g. 10, 50, 200). Defaults to 10.
1b	Should load balancing be used for parallelization? Users will likely want to set to FALSE for improved performance.

#### test.vc.twosigma

#### Value

A list with the following elements:

- fit\_null: Model fits under the null hypothesis. If return\_summary\_fits=TRUE, returns a list of objects of class summary.glmmTMB. If return\_summary\_fits=FALSE, returns a list of model fit objects of class glmmTMB. In either case, the order matches the row order of count\_matrix, and the names of the list elements are taken as the rownames of count\_matrix.
- fit\_alt: Model fits under the alt hypothesis of the same format as fit\_null.
- LR\_stat: Vector of Likelihood Ratio statistics. A value of 'NA' implies a convergence issue or other model fit problem.
- LR\_p.val: Vector of Likelihood Ratio p-values. A value of 'NA' implies a convergence issue or other model fit problem.

#### Details

If either model fails to converge, or the LR statistic is negative, both the statistic and p-value are assigned as NA.

#### Examples

# Set Parameters to Simulate Some Data

```
nind<-10;ncellsper<-rep(50,nind)
sigma.a<-.5;sigma.b<-.5;phi<-.1
alpha<-c(1,0,-.5,-2);beta<-c(2,0,-.1,.6)
beta2<-c(2,1,-.1,.6)
id.levels<-1:nind;nind<-length(id.levels)
id<-rep(id.levels,times=ncellsper)
sim.seed<-1234</pre>
```

```
# Simulate individual level covariates
```

```
t2d_sim<-rep(rbinom(nind,1,p=.4),times=ncellsper)
cdr_sim<-rbeta(sum(ncellsper),3,6)
age_sim<-rep(sample(c(20:60),size=nind,replace = TRUE),times=ncellsper)</pre>
```

# Construct design matrices

```
Z<-cbind(scale(t2d_sim),scale(age_sim),scale(cdr_sim))
colnames(Z)<-c("t2d_sim","age_sim","cdr_sim")
X<-cbind(scale(t2d_sim),scale(age_sim),scale(cdr_sim))
colnames(X)<-c("t2d_sim","age_sim","cdr_sim")</pre>
```

# Simulate Data

```
sim_dat<-matrix(nrow=2,ncol=sum(ncellsper))
for(i in 1:nrow(sim_dat)){
    sim_dat[i,]<-simulate_zero_inflated_nb_random_effect_data(ncellsper,X,Z,alpha,beta2
    ,phi,sigma.a,sigma.b,id.levels=NULL)$Y
}</pre>
```

```
rownames(sim_dat)<-paste("Gene",1:2)
# Run test.vc.twosigma
test.vc.twosigma(sim_dat[1,,drop=FALSE],mean_covar = X,zi_covar=Z
,mean_re = TRUE,zi_re=FALSE,id = id)</pre>
```

```
twosigma
```

Fit the TWO-SIGMA Model.

## Description

Fit the TWO-SIGMA Model.

## Usage

```
twosigma(
  count_matrix,
 mean_covar,
 zi_covar,
 mean_re = TRUE,
 zi_re = TRUE,
 id,
  adhoc = TRUE,
 adhoc_thresh = 0.1,
 return_summary_fits = TRUE,
 disp_covar = NULL,
 weights = rep(1, ncol(count_matrix)),
 control = glmmTMBControl(),
 ncores = 1,
 cluster_type = "Fork",
  chunk_size = 10,
  1b = FALSE
)
```

## Arguments

count_matrix	Matrix of non-negative integer read counts, with rows corresponding to genes and columns corresponding to cells. It is recommended to make the rownames the gene names for better output.
mean_covar	Covariates for the (conditional) mean model. Must be a matrix (without an intercept column) or $= 1$ to indicate an intercept only model.
zi_covar	Covariates for the zero-inflation model. Must be a matrix (without an intercept column), = 1 to indicate an intercept only model, or = 0 to indicate no zero-inflation model desired.
mean_re	Should random intercepts be included in the (conditional) mean model? Ignored if adhoc=TRUE.

zi_re	Should random intercepts be included in the zero-inflation model? Ignored if adhoc=TRUE.
id	Vector of individual-level ID's. Used for random effect prediction and the adhoc method but required regardless.
adhoc	Should the adhoc method be used by default to judge if random effects are needed?
adhoc_thresh	Value below which the adhoc p-value is deemed significant (and thus RE are deemed necessary). Only used if adhoc==TRUE.
return_summary_	_fits
	If TRUE, the package returns a summary.glmmTMB object for each gene. If FALSE, an object of class glmmTMB is returned for each gene. The latter requires far more memory to store.
disp_covar	Covariates for a log-linear model for the dispersion. Either a matrix of covariates or = 1 to indicate an intercept only model. Random effect terms are not permitted in the dispersion model. Defaults to NULL for constant dispersion.
weights	weights, as in glm. Defaults to 1 for all observations and no scaling or centering of weights is performed.
control	Control parameters for optimization in glmmTMB. See ?glmmTMBControl.
ncores	Number of cores used for parallelization. Defaults to 1, meaning no paralleliza- tion of any kind is done.
cluster_type	Whether to use a "cluster of type "Fork" or "Sock". On Unix systems, "Fork" will likely improve performance. On Windows, only "Sock" will actually result in parallelized computing.
chunk_size	Number of genes to be sent to each parallel environment. Parallelization is more efficient, particularly with a large count matrix, when the count matrix is 'chunked' into some common size (e.g. 10, 50, 200). Defaults to 10.
lb	Should load balancing be used for parallelization? Users will likely want to set to FALSE for improved performance.

## Value

A list with the following elements: ##'

- fit: If return\_summary\_fits=TRUE, returns a list of model fit objects of class summary.glmmTMB. If return\_summary\_fits=FALSE, returns a list of model fit objects of class glmmTMB. In either case, the order matches the row order of count\_matrix, and the names of the list elements are taken as the rownames of count\_matrix.
- adhoc\_include\_RE: Logical vector indicator whether the adhoc method determined random effects needed. If adhoc=F, then a vector of NA's.
- gene\_error: Vector indicating whether the particular gene produced an error during model fitting (TRUE) or not (FALSE).

## Details

If adhoc=TRUE, any input in mean\_re and zi\_re will be ignored.

## Examples

```
# Set Parameters to Simulate Some Data
```

```
nind<-10;ncellsper<-rep(50,nind)</pre>
sigma.a<-.5;sigma.b<-.5;phi<-.1</pre>
alpha<-c(1,0,-.5,-2);beta<-c(2,0,-.1,.6)
beta2<-c(2,1,-.1,.6)
id.levels<-1:nind;nind<-length(id.levels)</pre>
id<-rep(id.levels,times=ncellsper)</pre>
sim.seed<-1234
# Simulate individual level covariates
t2d_sim<-rep(rbinom(nind,1,p=.4),times=ncellsper)</pre>
cdr_sim<-rbeta(sum(ncellsper),3,6)</pre>
age_sim<-rep(sample(c(20:60), size=nind, replace = TRUE), times=ncellsper)</pre>
# Construct design matrices
Z<-cbind(scale(t2d_sim),scale(age_sim),scale(cdr_sim))</pre>
colnames(Z)<-c("t2d_sim","age_sim","cdr_sim")</pre>
X<-cbind(scale(t2d_sim), scale(age_sim), scale(cdr_sim))</pre>
colnames(X)<-c("t2d_sim","age_sim","cdr_sim")</pre>
# Simulate Data
sim_dat<-matrix(nrow=2,ncol=sum(ncellsper))</pre>
for(i in 1:nrow(sim_dat)){
   sim_dat[i,]<-simulate_zero_inflated_nb_random_effect_data(ncellsper,X,Z,alpha,beta2</pre>
   ,phi,sigma.a,sigma.b,id.levels=NULL)$Y
}
rownames(sim_dat)<-paste("Gene",1:2)</pre>
# Run twosigma
twosigma(sim_dat[1:2,],mean_covar = X,zi_covar=1,id = id)
```

twosigmag	Gene set testing for single-cell RNA-sequencing data adjusting for
	inter-gene correlation.

## Description

Gene set testing for single-cell RNA-sequencing data adjusting for inter-gene correlation.

#### Usage

twosigmag(
 count\_matrix,

## twosigmag

```
index_test,
index_ref = NULL,
all_as_ref = FALSE,
mean_form,
zi_form,
mean_form_null = NULL,
zi_form_null = NULL,
id,
statistic,
lr.df = NULL,
covar_to_test = NULL,
contrast_matrix = NULL,
factor_name = NULL,
rho = NULL,
allow_neg_corr = FALSE,
return_summary_fits = FALSE,
weights = NULL,
control = glmmTMBControl(),
ncores = 1,
cluster_type = "Fork",
chunk_size = 10,
lb = FALSE
```

## Arguments

)

count_matrix	Matrix of non-negative integer read counts. It is recommended to make the rownames the gene names for better output. No missing values can be present in the data.
index_test	List of indices corresponding to rows of the count matrix that are in the test set. Names of each list element (i.e. Gene Set Names) are carried forward to output if present.
index_ref	List of indices corresponding to rows of the count matrix that are in the reference set. If NULL, a reference set is randomly selected of the same size as the test size using genes not in the test set (if all_as_ref=FALSE) or using all other genes (if all_as_ref=TRUE). See all_as_ref. Must be either NULL or a list with the same length as index_test.
all_as_ref	Should all genes not in the test set be used as the reference? If FALSE, a random subset is taken of size equal to the test size.
mean_form	Two-sided model formula for the (conditional) mean model. Formula is passed directly into glmmTMB with random effects specified as in the lme4 package. Users should ensure that the LHS of the formula contains 'count '.
zi_form	One-sided model formula for the zero-inflation model under the alternative. For- mula is passed directly into glmmTMB with random effects specified as in the lme4 package.
mean_form_null	Two-sided model formula for the (conditional) mean model under the null. Needed if and only if statistic='LR'. Syntax is as in mean_form. Users should ensure that the LHS of the formula contains 'count'.

zi_form_null	One-sided model formula for the zero-inflation model under the null. Needed if and only if statistic='LR'. Syntax is as in zi_form.
id	Vector of individual-level (sample-level) ID's. Used to estimate inter-gene cor- relation and random effect prediction (if present) and is currently required.
statistic	Which gene-level statistic should be used. Options are Likelihood Ratio ("LR", default), Z-statistic from the mean model ("Z"),the Stouffer's method combined Z-statistic ("Stouffer"), or a contrast of regression parameters ("contrast"). If "Stouffer", covar_to_test must be in both components. If "contrast", covar_to_test is not used and must be NULL.
lr.df	degrees of freedom for the asymptotic chi-square approximation to the likeli- hood ratio statistic. Needed if and only if statistic='LR'.
covar_to_test	Covariate used for reporting direction (as Up or Down) of the test set and for col- lecting gene-level statistics. Either a string indicating the name of the covariate to use or an integer giving its associated position in the RHS of the mean_form argument. If a string, the name is matched to the predictors of the mean model, so users should ensure such a match would be unique. Not required and should be NULL if statistic='contrast'.
contrast_matri>	
	Matrix of contrasts of regression parameters from the mean model to be tested. Each row will have separate gene-level and set-level statistics. Rownames of contrast_matrix should correspond to a meaningful name of the hypothesis for nicely formatted output. If testing a factor, must have a number of columns exactly equal to the number of levels of the factor. Otherwise, must have one column per parameter in the mean model (including a column for the intercept.)
factor_name	Name of the factor being tested by contrast_matrix. Needed if and only if statistic='contrast' and contrast_matrix is testing a factor variable in the mean model.
rho	Inter-gene correlation value. If NULL (default), estimated using TWO-SIGMA model residuals.
allow_neg_corr	Should negative correlation values be allowed? If FALSE, negative correlations are set to zero (leads to conservative inference)
return_summary_	fits
	If TRUE, returns a list containing objects of class summary.glmmTMB for each gene.
weights	weights, as in glm. Defaults to 1 for all observations and no scaling or centering of weights is performed.
control	Control parameters for optimization in glmmTMB. See ?glmmTMBControl.
ncores	Number of cores used for parallelization. Defaults to 1, meaning no paralleliza- tion of any kind is done.
cluster_type	Whether to use a "cluster of type "Fork" or "Sock". On Unix systems, "Fork" will likely improve performance. On Windows, only "Sock" will actually result in parallelized computing.
chunk_size	Number of genes to be sent to each parallel environment. Parallelization is more efficient, particularly with a large count matrix, when the count matrix is 'chunked' into some common size (e.g. 10, 50, 200). Defaults to 10.

#### twosigmag

1b Should load balancing be used for parallelization? Users will likely want to set to FALSE for improved performance.

#### Value

A list with the following elements: ##'

- stats\_gene\_level\_all: Gives all gene-level statistics. Order matches the order of the inputted count matrix.
- p.vals\_gene\_level: Gives raw (unadjusted) p-values associated with stats\_gene\_level\_all.
- set\_p.val: Unadjusted set-level p-values. Order matches the order of inputted test sets.
- set\_p.val\_FDR: FDR-corrected (using the Benjamini-Hochberg procedure) set-level p-values. Order matches the order of inputted test sets.
- estimates\_gene\_level: Gives the average logFC or contrast estimate for each gene.
- se\_gene\_level: Standard error of the gene-level logFC values. Useful to construct gene-level summary statistics.
- estimates\_set\_level: Gives the set-level average of the gene-level logFC or contrast estimates.
- direction: Reports whether the test set tends to be Up or Down Regulated based on the sign of estimates\_set\_level.
- corr: Vector of estimated inter-gene correlations for each test set. Order matches the order of inputted test sets.
- gene\_level\_loglik: Vector of log-likelihood values for each gene. Values of NA indicates a model fitting or convergence problem for that gene.
- gene\_error: Vector indicating whether the particular gene produced an error during model fitting (TRUE) or not (FALSE).
- test\_sets: Vector of numeric indices corresponding to genes in each test set.
- ref\_sets: Vector of numeric indices corresponding to the genes in each reference set.
- gene\_summary\_fits: Summary.glmmTMB objects for each gene from the alternative model (if return\_summary\_fits=TRUE)

#### Examples

```
# Set Parameters to Simulate Some Data
```

```
nind<-10;ncellsper<-rep(50,nind)
sigma.a<-.5;sigma.b<-.5;phi<-.1
alpha<-c(1,0,-.5,-2);beta<-c(2,0,-.1,.6)
beta2<-c(2,1,-.1,.6)
id.levels<-1:nind;nind<-length(id.levels)
id<-rep(id.levels,times=ncellsper)
sim.seed<-1234</pre>
```

# Simulate individual level covariates

```
t2d_sim<-rep(rbinom(nind,1,p=.4),times=ncellsper)</pre>
```

```
cdr_sim<-rbeta(sum(ncellsper),3,6)</pre>
age_sim<-rep(sample(c(20:60),size=nind,replace = TRUE),times=ncellsper)</pre>
# Construct design matrices
Z<-cbind(scale(t2d_sim),scale(age_sim),scale(cdr_sim))</pre>
colnames(Z)<-c("t2d_sim","age_sim","cdr_sim")</pre>
X<-cbind(scale(t2d_sim),scale(age_sim),scale(cdr_sim))</pre>
colnames(X)<-c("t2d_sim","age_sim","cdr_sim")</pre>
# Simulate Data, half under null half under alternative
sim_dat<-matrix(nrow=4,ncol=sum(ncellsper))</pre>
for(i in 1:nrow(sim_dat)){
if(i<2){# Gene Sets Under the Null
   sim_dat[i,]<-simulate_zero_inflated_nb_random_effect_data(ncellsper,X,Z,alpha,beta2</pre>
   ,phi,sigma.a,sigma.b,id.levels=NULL)$Y
}else{# Gene Sets Under the Alternative
   sim_dat[i,]<-simulate_zero_inflated_nb_random_effect_data(ncellsper,X,Z,alpha,beta</pre>
   ,phi,sigma.a,sigma.b,id.levels=NULL)$Y
}
}
rownames(sim_dat)<-paste("Gene",1:4)</pre>
# Run twosigmag
twosigmag(sim_dat,index_test = list(c(1,3)),all_as_ref = TRUE,mean_form = count~X
,zi_form = ~0,id=id,covar_to_test = "t2d_sim",statistic = "Z")
```

twosigma_custom	Fit the TWO-SIGMA model with custom user-specified model formu-
	las.

#### Description

Fit the TWO-SIGMA model with custom user-specified model formulas.

## Usage

```
twosigma_custom(
  count_matrix,
  mean_form,
  zi_form,
  id,
  return_summary_fits = TRUE,
  silent = FALSE,
  disp_covar = NULL,
  weights = rep(1, ncol(count_matrix)),
  control = glmmTMBControl(),
```

## twosigma\_custom

```
ncores = 1,
cluster_type = "Fork",
chunk_size = 10,
lb = FALSE,
internal_call = FALSE
)
```

## Arguments

count_matrix	Matrix of non-negative integer read counts, with rows corresponding to genes and columns corresponding to cells. It is recommended to make the rownames the gene names for better output.
mean_form	Custom two-sided model formula for the (conditional) mean model. Formula is passed directly into glmmTMB with random effects specified as in the lme4 package. Users should ensure that the LHS of the formula begins with "count."
zi_form	Custom one-sided model formula for the zero-inflation model. Formula is passed directly into glmmTMB with random effects specified as in lme4.
id	Vector of individual-level (sample-level) ID's. Used for random effect predic- tion but required regardless of their presence in the model.
return_summary_	fits
	If TRUE, the package returns a summary.glmmTMB object for each gene. If FALSE, a glmmTMB object is returned for each gene. The latter requires far more storage space.
silent	If TRUE, progress is not printed.
disp_covar	Covariates for a log-linear model for the dispersion. Either a matrix of covariates $or = 1$ to indicate an intercept only model. Random effect terms are not permitted in the dispersion model.
weights	weights, as in glm. Defaults to 1 for all observations and no scaling or centering of weights is performed.
control	Control parameters for optimization in glmmTMB. See ?glmmTMBControl.
ncores	Number of cores used for parallelization. Defaults to 1, meaning no paralleliza- tion of any kind is done.
cluster_type	Whether to use a "cluster of type "Fork" or "Sock". On Unix systems, "Fork" will likely improve performance. On Windows, only "Sock" will actually result in parallelized computing.
chunk_size	Number of genes to be sent to each parallel environment. Parallelization is more efficient, particularly with a large count matrix, when the count matrix is 'chunked' into some common size (e.g. 10, 50, 200). Defaults to 10.
lb	Should load balancing be used for parallelization? Users will likely want to set to FALSE for improved performance.
internal_call	Not needed by users called twosigma_custom directly.

## Value

A list with the following elements:

- fit: If return\_summary\_fits=TRUE, returns a list of model fit objects of class summary.glmmTMB. If return\_summary\_fits=FALSE, returns a list of model fit objects of class glmmTMB. In either case, the order matches the row order of count\_matrix, and the names of the list elements are taken as the rownames of count\_matrix.
- gene\_error: Vector indicating whether the particular gene produced an error during model fitting (TRUE) or not (FALSE).

#### Details

This function is likely only needed if users wish to include random effect terms beyond random intercepts. Users should be confident in their abilities to specify random effects using the syntax of lme4.

## Examples

```
# Set Parameters to Simulate Some Data
```

```
nind<-10;ncellsper<-rep(50,nind)
sigma.a<-.5;sigma.b<-.5;phi<-.1
alpha<-c(1,0,-.5,-2);beta<-c(2,0,-.1,.6)
beta2<-c(2,1,-.1,.6)
id.levels<-1:nind;nind<-length(id.levels)
id<-rep(id.levels,times=ncellsper)
sim.seed<-1234</pre>
```

# Simulate individual level covariates

```
t2d_sim<-rep(rbinom(nind,1,p=.4),times=ncellsper)
cdr_sim<-rbeta(sum(ncellsper),3,6)
age_sim<-rep(sample(c(20:60),size=nind,replace = TRUE),times=ncellsper)</pre>
```

```
# Construct design matrices
```

```
Z<-cbind(scale(t2d_sim),scale(age_sim),scale(cdr_sim))
colnames(Z)<-c("t2d_sim","age_sim","cdr_sim")
X<-cbind(scale(t2d_sim),scale(age_sim),scale(cdr_sim))
colnames(X)<-c("t2d_sim","age_sim","cdr_sim")</pre>
```

```
# Simulate Data
```

```
sim_dat<-matrix(nrow=2,ncol=sum(ncellsper))
for(i in 1:nrow(sim_dat)){
    sim_dat[i,]<-simulate_zero_inflated_nb_random_effect_data(ncellsper,X,Z,alpha,beta2
    ,phi,sigma.a,sigma.b,id.levels=NULL)$Y
}
rownames(sim_dat)<-paste("Gene",1:2)</pre>
```

# Run twosigma\_custom

```
twosigma_custom(sim_dat[1:2,],mean_form = count~X,zi_form = ~0,id=id)
```

# Index